

Please write clearly in block capitals.

Centre number

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Candidate number

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Surname

Forename(s)

Candidate signature

I declare this is my own work.

AS MATHEMATICS

Paper 1

Thursday 18 May 2023

Afternoon

Time allowed: 1 hour 30 minutes

Materials

- You must have the AQA Formulae for A-level Mathematics booklet.
- You should have a graphical or scientific calculator that meets the requirements of the specification.

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer each question in the space provided for that question.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do **not** write outside the box around each page or on blank pages.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.

For Examiner's Use	
Question	Mark
1	
2	
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12	
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17	
18	
TOTAL	



J U N 2 3 7 3 5 6 1 0 1

Section AAnswer **all** questions in the spaces provided.

- 1** At a point P on a curve, the gradient of the tangent to the curve is 10

State the gradient of the normal to the curve at P

Circle your answer.

[1 mark]

-10

-0.1

0.1

10

- 2** Identify the expression below which is equivalent to $\left(\frac{2x}{5}\right)^{-3}$

Circle your answer.

[1 mark]

$$\frac{8x^3}{125}$$

$$\frac{125x^3}{8}$$

$$\frac{125}{8x^3}$$

$$\frac{8}{125x^3}$$



3

The coefficient of x^2 in the binomial expansion of $(1 + ax)^6$ is $\frac{20}{3}$

Find the two possible values of a

[3 marks]

Turn over for the next question

Turn over ►



4 It is given that $5 \cos^2 \theta - 4 \sin^2 \theta = 0$

4 (a) Find the possible values of $\tan \theta$, giving your answers in exact form.

[3 marks]

4 (b) Hence, or otherwise, solve the equation

$$5 \cos^2 \theta - 4 \sin^2 \theta = 0$$

giving all solutions of θ to the nearest 0.1° in the interval $0^\circ \leq \theta \leq 360^\circ$

[2 marks]



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[2 marks]

Find the value of k

[5 marks]

[illegible]

6 (a) The curve C_1 has equation $y = 2x^2 - 20x + 42$

Express the equation of C_1 in the form

$$y = a(x - b)^2 + c$$

where a , b and c are integers.

[3 marks]

6 (b) Write down the coordinates of the minimum point of C_1

[1 mark]

6 (c) The curve C_1 is mapped onto the curve C_2 by a stretch in the y -direction.

The minimum point of C_2 is at $(5, -4)$

Find the equation of C_2

[2 marks]



7 Points P and Q lie on the curve with equation $y = x^4$

The x -coordinate of P is x

The x -coordinate of Q is $x + h$

7 (a) Expand $(x + h)^4$

[2 marks]

7 (b) Hence, find an expression, in terms of x and h , for the gradient of the line PQ

[1 mark]

7 (c) Explain how to use the answer from part **(b)** to obtain the gradient function of $y = x^4$

[2 marks]

Turn over ►



8 (a) Show that

$$\int_1^a \left(6 - \frac{12}{\sqrt{x}}\right) dx = 6a - 24\sqrt{a} + 18$$

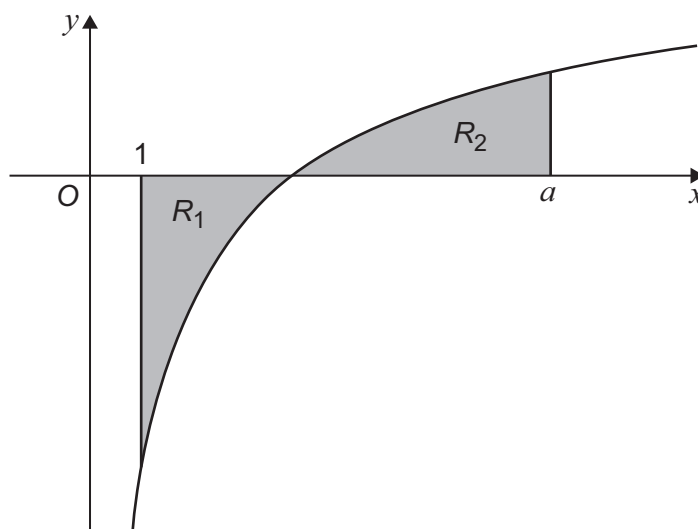
[3 marks]



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The shaded region R_2 is bounded by the curve, the line $x = a$ and the x -axis.



Fully justify your answer.

[4 marks]

[illegible]

Turn over ►



9

A continuous curve has equation $y = f(x)$

The curve passes through the points $A(2, 1)$, $B(4, 5)$ and $C(6, 1)$

It is given that $f'(4) = 0$

Jasmin made two statements about the nature of the curve $y = f(x)$ at the point B :

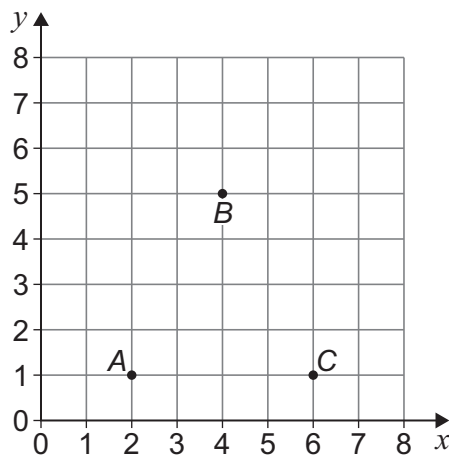
Statement 1: There is a turning point at B

Statement 2: There is a maximum point at B

9 (a)

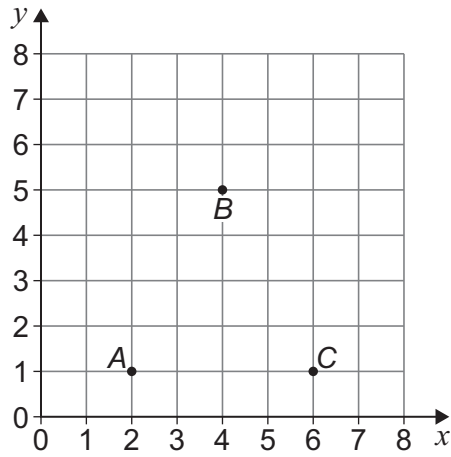
Draw a sketch of the curve $y = f(x)$ such that Statement 1 is correct and Statement 2 is correct.

[1 mark]



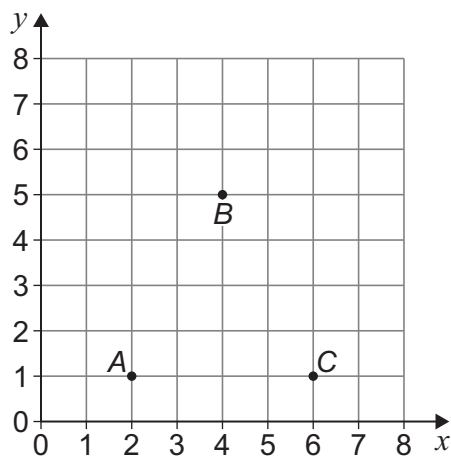
- 9 (b) Draw a sketch of the curve $y = f(x)$ such that Statement 1 is correct and Statement 2 is **not** correct.

[1 mark]



- 9 (c) Draw a sketch of the curve $y = f(x)$ such that Statement 1 is **not** correct and Statement 2 is **not** correct.

[1 mark]



Turn over ►



10 Charlie buys a car for £18 000 on 1 January 2016.

The value of the car decreases exponentially.

The car has a value of £12 000 on 1 January 2018.

10 (a) Charlie says:

- because the car has lost £6000 after two years, after another two years it will be worth £6000.

Charlie's friend Kaya says:

- because the car has lost one third of its value after two years, after another two years it will be worth £8000.

Explain whose statement is correct, justifying the value they have stated.

[2 marks]



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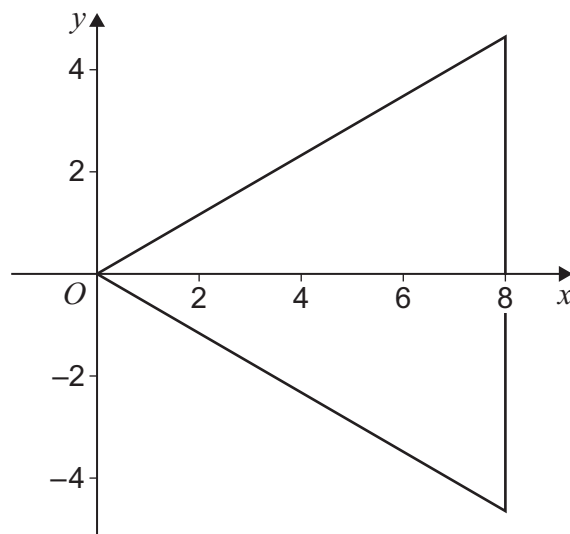
- 11 (a)** A circle has equation

$$x^2 + y^2 - 10x - 6 = 0$$

Find the centre and the radius of the circle.

[2 marks]

- 11 (b)** An equilateral triangle has one vertex at the origin, and one side along the line $x = 8$, as shown in the diagram below.



- 11 (b) (i)** Show that the vertex at the origin lies inside the circle $x^2 + y^2 - 10x - 6 = 0$

[1 mark]



[4 marks]

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Section BAnswer **all** questions in the spaces provided.

- 12** A particle, initially at rest, starts to move forward in a straight line with constant acceleration, $a \text{ m s}^{-2}$

After 6 seconds the particle has a velocity of 3 m s^{-1}

Find the value of a

Circle your answer.

[1 mark]

-2

-0.5

0.5

2

- 13** A resultant force of $\begin{bmatrix} -2 \\ 6 \end{bmatrix} \text{ N}$ acts on a particle.

The acceleration of the particle is $\begin{bmatrix} -6 \\ y \end{bmatrix} \text{ m s}^{-2}$

Find the value of y

Circle your answer.

[1 mark]

2

3

10

18



- 14** A ball, initially at rest, is dropped from a vertical height of h metres above the Earth's surface.

After 4 seconds the ball's height above the Earth's surface is $0.2h$ metres.

- 14 (a)** Assuming air resistance can be ignored, show that

$$h = 10g$$

[3 marks]

- 14 (b)** Assuming air resistance cannot be ignored, explain the effect that this would have on the value of h in part (a).

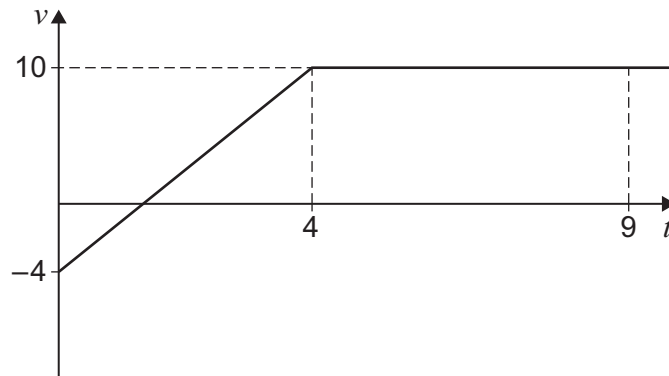
[1 mark]

Turn over ►



15

A particle is moving in a straight line such that its velocity, $v \text{ m s}^{-1}$, changes with respect to time, t seconds, as shown in the graph below.



15 (a)

Show that the acceleration of the particle over the first 4 seconds is 3.5 m s^{-2}

[1 mark]

15 (b)

The particle is initially at a fixed point P

Show that the displacement of the particle from P , when $t = 9$, is 62 metres.

[3 marks]



- 16** A toy remote control speed boat is launched from one edge of a small pond and moves in a straight line across the pond's surface.

The boat's velocity, $v \text{ m s}^{-1}$, is modelled in terms of time, t seconds after the boat is launched, by the expression

$$v = 0.9 + 0.16t - 0.06t^2$$

- 16 (a)** Find the acceleration of the boat when $t = 2$

[3 marks]

- 16 (b)** Find the displacement of the boat, from the point where it was launched, when $t = 2$

[4 marks]

Turn over ►



17 A particle, P , is initially at rest on a smooth horizontal surface.

A resultant force of $\begin{bmatrix} 12 \\ 9 \end{bmatrix}$ N is then applied to P , so that it moves in a straight line.

17 (a) Find the magnitude of the resultant force.

[1 mark]

17 (b) Two fixed points A and B have position vectors

$$\overrightarrow{OA} = \begin{bmatrix} 3 \\ 7 \end{bmatrix} \text{ metres} \quad \text{and} \quad \overrightarrow{OB} = \begin{bmatrix} k \\ k-1 \end{bmatrix} \text{ metres}$$

with respect to a fixed origin, O

P moves in a straight line parallel to \overrightarrow{AB}

17 (b) (i) Find \overrightarrow{AB} in terms of k

[1 mark]



17 (b) (ii) Find the value of k

[2 marks]

Turn over for the next question

Turn over ►



18 (b)

State one assumption that must be made in answering part (a).

[1 mark]**END OF QUESTIONS**

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[illegible]

[illegible]

[illegible]

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