

Please write clearly in block capitals.

Centre number

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Candidate number

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Surname

Forename(s)

Candidate signature

A-level MATHEMATICS

Paper 1

Wednesday 6 June 2018

Morning

Time allowed: 2 hours

Materials

- You must have the AQA Formulae for A-level Mathematics booklet.
- You should have a graphical or scientific calculator that meets the requirements of the specification.

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer each question in the space provided for that question. If you require extra space, use an AQA supplementary answer book; do **not** use the space provided for a different question.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 100.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.

For Examiner's Use	
Question	Mark
1	
2	
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9	
10	
11	
12	
13	
14	
15	
TOTAL	



Answer **all** questions in the spaces provided.

1

$$y = \frac{1}{x^2}$$

Find an expression for $\frac{dy}{dx}$

Circle your answer.

[1 mark]

$$\frac{dy}{dx} = \frac{0}{2x}$$

$$\frac{dy}{dx} = x^{-2}$$

$$\frac{dy}{dx} = -\frac{2}{x}$$

$$\frac{dy}{dx} = -\frac{2}{x^3}$$

2

The graph of $y = 5^x$ is transformed by a stretch in the y -direction, scale factor 5

State the equation of the transformed graph.

Circle your answer.

[1 mark]

$$y = 5 \times 5^x$$

$$y = 5^{\frac{x}{5}}$$

$$y = \frac{1}{5} \times 5^x$$

$$y = 5^{5x}$$



3 A periodic sequence is defined by $U_n = \sin\left(\frac{n\pi}{2}\right)$

State the period of this sequence.

Circle your answer.

[1 mark]

8

2π

4

π

4 The function f is defined by $f(x) = e^{x-4}$, $x \in \mathbb{R}$

Find $f^{-1}(x)$ and state its domain.

[3 marks]

Turn over for the next question

Turn over ►



5 A curve is defined by the parametric equations

$$x = 4 \times 2^{-t} + 3$$

$$y = 3 \times 2^t - 5$$

5 (a) Show that $\frac{dy}{dx} = -\frac{3}{4} \times 2^{2t}$

[3 marks]

5 (b) Find the Cartesian equation of the curve in the form $xy + ax + by = c$, where a , b and c are integers.

[3 marks]



- 6 (a)** Find the first three terms, in ascending powers of x , of the binomial expansion
of $\frac{1}{\sqrt{4+x}}$

[3 marks]

- 6 (b)** Hence, find the first three terms of the binomial expansion of $\frac{1}{\sqrt{4-x^3}}$

[2 marks]

Question 6 continues on the next page

Turn over ►

- 6 (c)** Using your answer to part **(b)**, find an approximation for $\int_0^1 \frac{1}{\sqrt{4-x^3}} dx$, giving your answer to seven decimal places.

[3 marks]

- 6 (d) (i)** Edward, a student, decides to use this method to find a more accurate value for the integral by increasing the number of terms of the binomial expansion used.

Explain clearly whether Edward's approximation will be an overestimate, an underestimate, or if it is impossible to tell.

[2 marks]



6 (d) (ii) Edward goes on to use the expansion from part **(b)** to find an approximation

for $\int_{-2}^0 \frac{1}{\sqrt{4-x^3}} dx$

Explain why Edward's approximation is invalid.

[2 marks]

Turn over for the next question



7 Three points A , B and C have coordinates $A(8, 17)$, $B(15, 10)$ and $C(-2, -7)$

7 (a) Show that angle ABC is a right angle.

[3 marks]

7 (b) A , B and C lie on a circle.

7 (b) (i) Explain why AC is a diameter of the circle.

[1 mark]

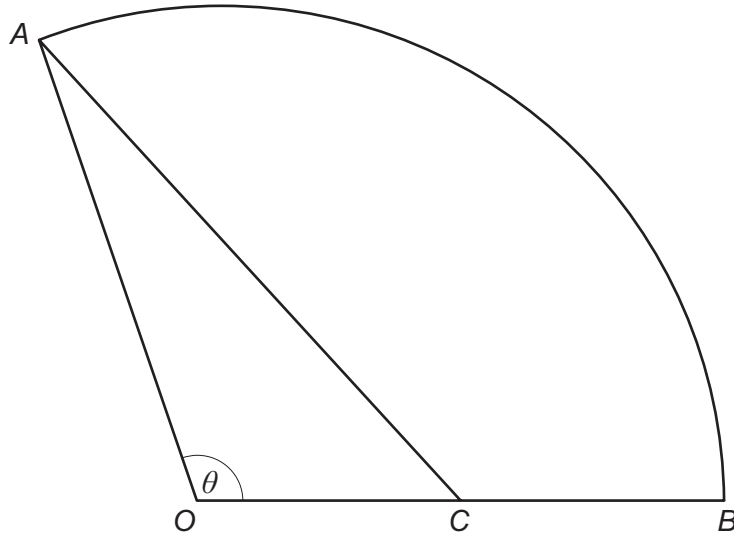


8

The diagram shows a sector of a circle OAB .

C is the midpoint of OB .

Angle AOB is θ radians.



8 (a)

Given that the area of the triangle OAC is equal to one quarter of the area of the sector OAB , show that $\theta = 2 \sin \theta$

[4 marks]



- 8 (b)** Use the Newton-Raphson method with $\theta_1 = \pi$, to find θ_3 as an approximation for θ .
Give your answer correct to five decimal places.

[3 marks]

- 8 (c)** Given that $\theta = 1.89549$ to five decimal places, find an estimate for the percentage error in the approximation found in part (b).

[1 mark]

Turn over for the next question

Turn over ►



10 (b) The scientist wants the mass of caffeine in her body to stay below 480 mg
Use the model to find the earliest time that she could drink another cup of strong coffee.

Give your answer to the nearest minute.

[3 marks]

10 (c) State a reason why the mass of caffeine remaining in the scientist's body predicted by the model may not be accurate.

[1 mark]

Turn over for the next question

Turn over ►



12 $p(x) = 30x^3 - 7x^2 - 7x + 2$

12 (a) Prove that $(2x + 1)$ is a factor of $p(x)$

[2 marks]

12 (b) Factorise $p(x)$ completely.

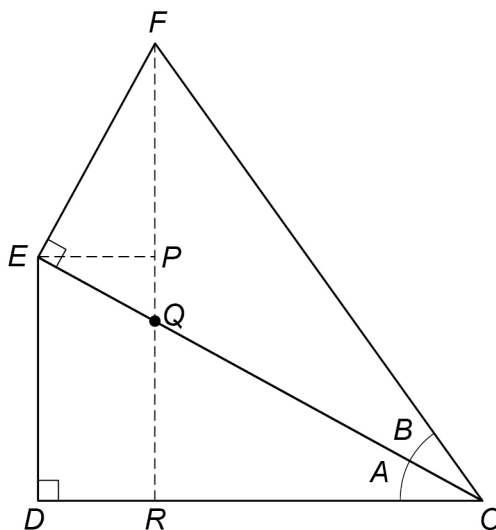
[3 marks]



14

Some students are trying to prove an identity for $\sin(A + B)$.

They start by drawing two right-angled triangles ODE and OEF , as shown.



The students' incomplete proof continues,

Let angle $DOE = A$ and angle $EOF = B$.

In triangle OFR ,

Line 1	$\sin(A + B) = \frac{RF}{OF}$
Line 2	$= \frac{RP + PF}{OF}$
Line 3	$= \frac{DE}{OF} + \frac{PF}{OF}$ since $DE = RP$
Line 4	$= \frac{DE}{\dots} \times \frac{\dots}{OF} + \frac{PF}{EF} \times \frac{EF}{OF}$
Line 5	$= \dots + \cos A \sin B$

14 (a) Explain why $\frac{PF}{EF} \times \frac{EF}{OF}$ in Line 4 leads to $\cos A \sin B$ in Line 5

[2 marks]



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14 (b) Complete Line 4 and Line 5 to prove the identity

Line 4 $= \frac{DE}{\dots} \times \frac{\dots}{OF} + \frac{PF}{EF} \times \frac{EF}{OF}$

Line 5 $= \dots + \cos A \sin B$ **[1 mark]**

14 (c) Explain why the argument used in part (a) only proves the identity when A and B are acute angles. **[1 mark]**

14 (d) Another student claims that by replacing B with $-B$ in the identity for $\sin(A + B)$ it is possible to find an identity for $\sin(A - B)$.

Assuming the identity for $\sin(A + B)$ is correct for all values of A and B , prove a similar result for $\sin(A - B)$. **[3 marks]**

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Turn over ►



15 A curve has equation $y = x^3 - 48x$

The point A on the curve has x coordinate -4

The point B on the curve has x coordinate $-4 + h$

15 (a) Show that the gradient of the line AB is $h^2 - 12h$

[4 marks]

15 (b) Explain how the result of part **(a)** can be used to show that A is a stationary point on the curve.

[2 marks]

END OF QUESTIONS



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2 5

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