

| Please write clearly in | ı block capitals. | |
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| Centre number | Candidate number | |
| Surname | | - |
| Forename(s) | | - |
| Candidate signature | I declare this is my own work. | - / |

A-level **MATHEMATICS**

Paper 3

Time allowed: 2 hours

Materials

- You must have the AQA Formulae for A-level Mathematics booklet.
- You should have a graphical or scientific calculator that meets the requirements of the specification.

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer all questions.
- You must answer each question in the space provided for that question. If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 100.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.

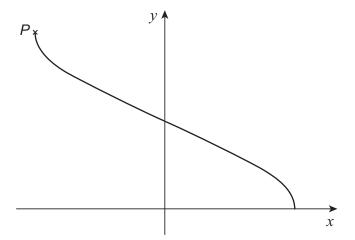
| For Exam | iner's Use |
|----------|------------|
| Question | Mark |
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Section A

Answer all questions in the spaces provided.

1 The graph of $y = \arccos x$ is shown.



State the coordinates of the end point *P*.

Circle your answer.

[1 mark]

$$(-\pi, 1)$$

$$(-1, \pi)$$

$$\left(-\pi,\;1\right) \hspace{1cm} \left(-1,\;\pi\right) \hspace{1cm} \left(-\frac{\pi}{2},\;1\right) \hspace{1cm} \left(-1,\;\frac{\pi}{2}\right)$$

$$\left(-1, \frac{\pi}{2}\right)$$

2 Simplify fully

$$\frac{(x+3)(6-2x)}{(x-3)(3+x)}$$
 for $x \neq \pm 3$

Circle your answer.

[1 mark]

$$\frac{(6-2x)}{(x-3)}$$

$$\frac{(6-2x)}{(x-3)}$$
 $\frac{(2x-6)}{(x-3)}$

3
$$f(x) = 3x^2$$

Obtain
$$\lim_{h\to 0} \frac{f(x+h) - f(x)}{h}$$

Circle your answer.

[1 mark]

$$\frac{3h^2}{h}$$

$$\frac{3(x+h)^2-3x^2}{h}$$



| Find Personal Tutor from www.wisesprout.co.uk |
|---|
| 找名校导师,用小草线上辅导(微信小程序同名) |

| 4 (a) | Show that the first three terms, in descending powers of x , of the expansion of | |
|-------|--|--------|
| | $(2x-3)^{10}$ | |
| | are given by | |
| | $1024x^{10} + px^9 + qx^8$ | |
| | | |
| | where p and q are integers to be found. [3 m | narks] |
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| 4 (b) | Find the constant term in the expansion of | |
| | $\left(2x-\frac{3}{x}\right)^{10}$ | |
| | $\langle \lambda \rangle$ | |
| | [2 m | narks] |
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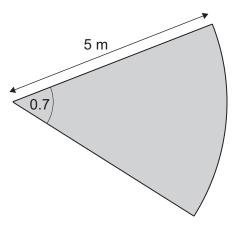


5 A gardener is creating flowerbeds in the shape of sectors of circles.

The gardener uses an edging strip around the perimeter of each of the flowerbeds.

The cost of the edging strip is £1.80 per metre and can be purchased for any length.

One of the flowerbeds has a radius of 5 metres and an angle at the centre of 0.7 radians as shown in the diagram below.



| 5 | (a) | /i) | Find · | the | area | ٥f | this | flowerbed | 4 |
|---|-----|-----|--------|------|------|----|------|-----------|---|
| ບ | (a) | (1) | FILIU | เมเษ | arta | UΙ | นแธ | liowerped | ı |

| | | [Z marks] |
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Question 5 continues on the next page



| 5 (a) (ii) | Find the cost of the edging strip required for this flowerbed. [3 marks] |
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| 5 (b) | A flowerbed is to be made with an area of 20 m ² |
| 5 (b) (i) | Show that the cost, £ C , of the edging strip required for this flowerbed is given by |
| o (b) (i) | |
| | $C = \frac{18}{5} \left(\frac{20}{r} + r \right)$ |
| | where r is the radius measured in metres. [3 marks] |
| | [5 marks] |
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| 5 (b) (ii) | Hence, show that the minimum cost of the edging strip for this flowerbed occurs |
|------------|---|
| · () | when $r \approx 4.5$ |
| | when $r \approx 4.5$ |
| | |
| | Fully justify your answer. |
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| | [5 marks] |
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| 6 | Given that $x > 0$ and $x \neq 25$, fu | | |
|---|---|---|-----------|
| | | $\frac{10 + 5x - 2x^{\frac{1}{2}} - x^{\frac{3}{2}}}{5 - \sqrt{x}}$ | |
| | Fully justify your answer. | | [4 marks] |
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| 7 | A building has a leaking roof and, while it is raining, water drips into a 12 litre bucket. |
|--------------|---|
| | When the rain stops, the bucket is one third full. |
| | Water continues to drip into the bucket from a puddle on the roof. |
| | In the first minute after the rain stops, 30 millilitres of water drips into the bucket. |
| | In each subsequent minute, the amount of water that drips into the bucket reduces by 2%. |
| | During the n th minute after the rain stops, the volume of water that drips into the bucket is W_n millilitres. |
| 7 (a) | Find W_2 [1 mark] |
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| 7 (b) | Explain why |
| <i>i</i> (b) | |
| | $W_n = A 	imes 0.98^{n-1}$ |
| | and state the value of A . [2 marks] |
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| 7 (c) | Find the increase in the water in the bucket 15 minutes after the rain stops. | |
|-------|---|-----------|
| | Give your answer to the nearest millilitre. | |
| | | [2 marks] |
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| 7 (d) | Assuming it does not start to rain again, find the maximum amount of water | in the |
| | bucket. | [3 marks] |
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| 7 (e) | After several hours the water has stopped dripping. | |
| | Give two reasons why the amount of water in the bucket is not as much as | the |
| | answer found in part (d). | [2 marks] |
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| 8 | Given that |
|---|---|
| | $\int_{\frac{\pi}{4}}^{\frac{\pi}{3}} x \cos x \mathrm{d}x = a\pi + b$ |
| | find the exact value of a and the exact value of b . |
| | Fully justify your answer. [6 marks] |
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| 9 | A function f is defined for all real values of x as | |
|------------|---|-----------|
| | $f(x) = x^4 + 5x^3$ | |
| | The function has exactly two stationary points when $x = 0$ and $x = -\frac{15}{4}$ | |
| 9 (a) (i) | Find $f''(x)$ | |
| | | [2 marks] |
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| 9 (a) (ii) | Determine the nature of the stationary points. | |
| - (, (, | Fully justify your answer. | |
| | Tany judany your anower. | [4 marks] |
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| 9 (b) | State the range of values of <i>x</i> for which | |
|------------|---|----------|
| | $f(x) = x^4 + 5x^3$ | |
| | is an increasing function. | |
| | | [1 mark] |
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| 0 (=) | A accord function a in defined for all real values of a se | |
| 9 (c) | A second function g is defined for all real values of x as | |
| | $g(x) = x^4 - 5x^3$ | |
| 9 (c) (i) | State the single transformation which maps f onto g. | |
| | | [1 mark] |
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| 0 () (") | | |
| 9 (c) (II) | State the range of values of x for which g is an increasing function. | [1 mark] |
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| | | Section | В | | |
|----|--|------------------|-----------------------|-------------------|------|
| | Answer all qu | estions in th | e spaces provided. | | |
| 10 | Anke has collected data from between the age of the car an | | | e any correlation | |
| | She calculates the correlation | coefficient. | | | |
| | Which of the following statement | ents best de | scribes her answer of | -1.2? | |
| | Tick (✓) one box. | | | [1 m | ark] |
| | Definitely incorrect | | | | |
| | Probably incorrect | | | | |
| | Probably correct | | | | |
| | Definitely correct | | | | |
| 11 | The random variable X is such | h that $X\sim$ E | $\beta(n, p)$ | | |
| | The mean value of X is 225 | | | | |
| | The variance of X is 144 | | | | |
| | Find p . | | | | |
| | Circle your answer. | | | [1 m | ark1 |
| | 0.36 | 0.6 | 0.64 | 0.8 | |
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| 12 | An electoral register contains 8000 names. | |
|----|--|--------|
| | A researcher decides to select a systematic sample of 100 names from the reg | ister. |
| | Explain how the researcher should select such a sample. [3] | marks] |
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13 The table below is an extract from the Large Data Set.

| Propulsion Type | Region | Engine Size | Mass | CO ₂ | Particulate Emissions |
|--------------------|------------|-------------|------|-----------------|--------------------------|
| 2 | London | 1896 | 1533 | 154 | 0.04 |
| 2 | North West | 1896 | 1423 | 146 | 0.029 |
| 2 | North West | 1896 | 1353 | 138 | 0.025 |
| 2 | South West | 1998 | 1547 | 159 | 0.026 |
| 2 | London | 1896 | 1388 | 138 | 0.025 |
| 2 | South West | 1896 | 1214 | 130 | 0.011 |
| 2 | South West | 1896 | 1480 | 146 | 0.029 |
| 2 | South West | 1896 | 1413 | 146 | 0.024 |
| 2 | South West | 2496 | 1695 | 192 | 0.034 |
| 2 | South West | 1422 | 1251 | 122 | 0.025 |
| 2 | South West | 1995 | 2075 | 175 | 0.034 |
| 2 | London | 1896 | 1285 | 140 | 0.036 |
| 2 | North West | 1896 | 0 | 146 | |

| 13 (a) (I) | Calculate the mean and standard deviation of CO ₂ emissions in the table. | [2 marks] |
|------------|--|-----------|
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| 13 (a) (ii) | Any value more than 2 standard deviations from the mean can be identified as an outlier. | | |
|-------------|---|-----------|--|
| | Determine, using this definition of an outlier, if there are any outliers in this ${\rm CO}_2$ emissions. | sample of | |
| | Fully justify your answer. | [2 marks] | |
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| 13 (b) | Maria claims that the last line in the table must contain two errors. | | |
| | Use your knowledge of the Large Data Set to comment on Maria's claim. | [2 marks] | |
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| | Turn over for the next question | | |
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| 14 | A and B are two events such the | nat | |
|--------|-----------------------------------|---------------------|-----------|
| | | $P(A \cap B) = 0.1$ | |
| | | $P(A'\cap B')=0.2$ | |
| | | P(B) = 2P(A) | |
| 14 (a) | Find P(A) | | |
| | | | [4 marks] |
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| 14 (b) | Find $P(B A)$ | | [2 marks] |
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| 14 (c) | Determine if A and B are independent events. | [1 mark] |
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Turn over for the next question



Turn over ▶

| 15 | A team game involves solving puzzles to escape from a room. | | |
|----|--|--|--|
| | Using data from the past, the mean time to solve the puzzles and escape from one of these rooms is 65 minutes with a standard deviation of 11.3 minutes. | | |
| | After recent changes to the puzzles in the room, it is claimed that the mean time to solve the puzzles and escape has changed. | | |
| | To test this claim, a random sample of 100 teams is selected. | | |
| | The total time to solve the puzzles and escape for the 100 teams is 6780 minutes. | | |
| | Assuming that the times are normally distributed, test at the 2% level the claim that the mean time has changed. | | |
| | [7 marks | | |
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16 The discrete random variable *X* has the probability function

$$P(X = x) = \begin{cases} c(7 - 2x) & x = 0, 1, 2, 3 \\ k & x = 4 \\ 0 & \text{otherwise} \end{cases}$$

where c and k are constants.

| 16 (a |) Show tha | 16c + k = 1 |
|-------|------------|-------------|
| | | |

[2 marks]

| 16 (b) | Given that | D(Y > | > 3) — | 5 |
|--------|------------|------------------|--------|---|
| 10 (b) | Given that | Γ (Λ <u><</u> | _ 3) — | 8 |

find the value of c and the value of k.

[2 marks]

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| 17 | James is playing a mathematical game on his computer. | |
|--------|---|-----------|
| | The probability that he wins is 0.6 | |
| | As part of an online tournament, James plays the game 10 times. | |
| | Let <i>Y</i> be the number of games that James wins. | |
| 17 (a) | State two assumptions, in context, for Y to be modelled as $B(10, 0.6)$ | [2 marks] |
| | | |
| | | |
| 17 (b) | Find $P(Y=4)$ | [1 mark] |
| | | |
| 17 (c) | Find $P(Y \ge 4)$ | [2 marks] |
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| 17 (d) | After practising the game, James claims that he has increased his probability of winning the game. | of |
|--------|--|--------|
| | In a random sample of 15 subsequent games, he wins 12 of them. | |
| | Test a 5% significance level whether James's claim is correct. [6] | marks] |
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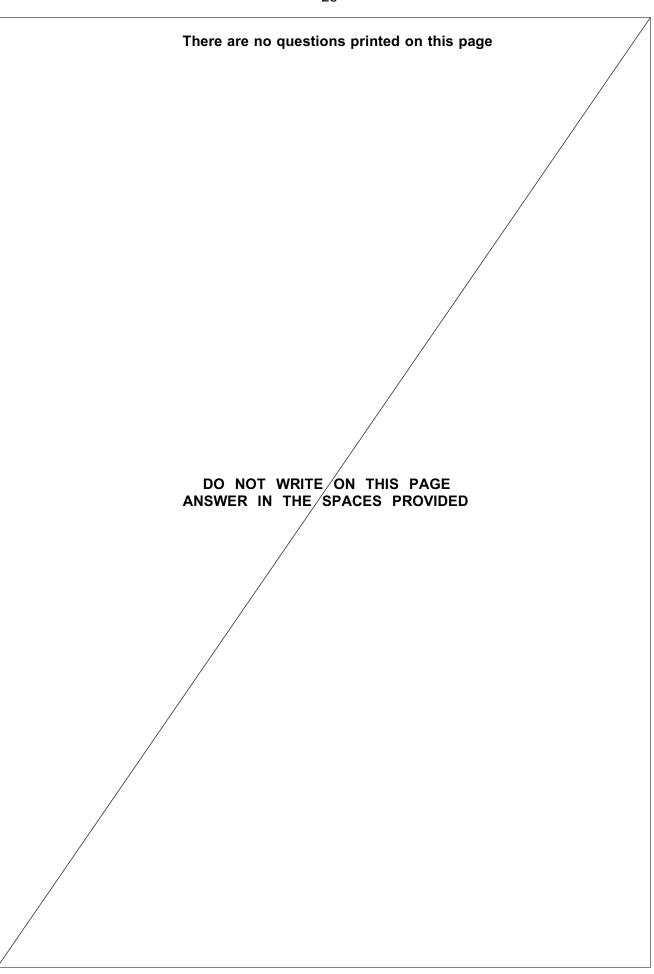


| 18 | A factory produces jars of jam and jars of marmalade. |
|-------------|---|
| 18 (a) | The weight, X grams, of jam in a jar can be modelled as a normal variable with mean 372 and a standard deviation of 3.5 |
| 18 (a) (i) | Find the probability that the weight of jam in a jar is equal to 372 grams. [1 mark] |
| | |
| 18 (a) (ii) | Find the probability that the weight of jam in a jar is greater than 368 grams. [2 marks] |
| | |
| | |
| | |
| 18 (b) | The weight, Y grams, of marmalade in a jar can be modelled as a normal variable with mean μ and standard deviation σ |
| 18 (b) (i) | Given that $P(Y < 346) = 0.975$, show that |
| | $346-\mu=1.96\sigma$ |
| | Fully justify your answer. [3 marks] |
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| 40 (b) (;;) | Civan further that |
|-------------|-------------------------|
| 18 (B) (II) | Given further that |
| | P(Y < 336) = 0.14 |
| | 1 (1 < 000) = 0.17 |
| | find μ and σ |
| | [4 marks] |
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