

GCE

Mathematics A

H240/02: Pure Mathematics and Statistics

Advanced GCE

Mark Scheme for November 2020

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

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Text Instructions

1. Annotations and abbreviations

Annotation in RM assessor	Meaning
√and ×	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
۸	Omission sign
MR	Misread
BP	Blank Page
Seen	
Highlighting	
Other abbreviations in	Meaning
mark scheme	
dep*	Mark dependent on a previous mark, indicated by *. The * may be omitted if only one previous M mark
cao	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working
AG	Answer given
awrt	Anything which rounds to
BC	By Calculator
DR	This question included the instruction: In this question you must show detailed reasoning.

Mark Scheme

2. Subject-specific Marking Instructions for A Level Mathematics A

a Annotations must be used during your marking. For a response awarded zero (or full) marks a single appropriate annotation (cross, tick, M0 or ^) is sufficient, but not required.

For responses that are not awarded either 0 or full marks, you must make it clear how you have arrived at the mark you have awarded and all responses must have enough annotation for a reviewer to decide if the mark awarded is correct without having to mark it independently.

It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

Award NR (No Response)

- if there is nothing written at all in the answer space and no attempt elsewhere in the script
- OR if there is a comment which does not in any way relate to the question (e.g. 'can't do', 'don't know')
- OR if there is a mark (e.g. a dash, a question mark, a picture) which isn't an attempt at the question.

Note: Award 0 marks only for an attempt that earns no credit (including copying out the question).

If a candidate uses the answer space for one question to answer another, for example using the space for 8(b) to answer 8(a), then give benefit of doubt unless it is ambiguous for which part it is intended.

b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not always be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner. If you are in any doubt whatsoever you should contact your Team Leader.

c The following types of marks are available.

Μ

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

A method mark may usually be implied by a correct answer unless the question includes the DR statement, the command words "Determine" or "Show that", or some other indication that the method must be given explicitly.

Α

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

В

Mark for a correct result or statement independent of Method marks.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- e The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case please, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.

Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

- f We are usually quite flexible about the accuracy to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so.
 - When a value is given in the paper only accept an answer correct to at least as many significant figures as the given value.

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- When a value **is not given** in the paper accept any answer that agrees with the correct value to **3 s.f.** unless a different level of accuracy has been asked for in the question, or the mark scheme specifies an acceptable range.
 - NB for Specification B (MEI) the rubric is not specific about the level of accuracy required, so this statement reads "2 s.f".

Follow through should be used so that only one mark in any question is lost for each distinct accuracy error.

Candidates using a value of 9.80, 9.81 or 10 for *g* should usually be penalised for any final accuracy marks which do not agree to the value found with 9.8 which is given in the rubric.

- g Rules for replaced work and multiple attempts:
 - If one attempt is clearly indicated as the one to mark, or only one is left uncrossed out, then mark that attempt and ignore the others.
 - If more than one attempt is left not crossed out, then mark the last attempt unless it only repeats part of the first attempt or is substantially less complete.
 - if a candidate crosses out all of their attempts, the assessor should attempt to mark the crossed out answer(s) as above and award marks appropriately.
- For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A or B mark in the question. Marks designated as cao may be awarded as long as there are no other errors. If a candidate corrects the misread in a later part, do not continue to follow through. Note that a miscopy of the candidate's own working is not a misread but an accuracy error.
- i If a calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers, provided that there is nothing in the wording of the question specifying that analytical methods are required such as the bold "In this question you must show detailed reasoning", or the command words "Show" or "Determine". Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.
- j If in any case the scheme operates with considerable unfairness consult your Team Leader.

	Question		Answer	Mark	AO	Guidance
1	(a)	(i)	$14(2x+3)^6$ oe	M1	1.1	M1 for $k(2x+3)^6$ or $14u^6$ seen
				A1	1.1	A1 all correct ISW
				[2]		
1	(a)	(ii)	$3x^2\ln x + x^2$ oe	M1	1.1	Attempt use product rule; allow incorrect sign; allow $\ln x 3x^2 + x^2$
				A1	1.1	One term correct
				A1 [3]	1.1	All correct ISW eg factorised incorrectly
1	(b)		$\frac{1}{5}\sin 5x \qquad (+c)$	M1	1.1	M1 for $\sin 5x$ seen NOT $-5\sin 5x$
				A1 [2]	1.1	A1 all correct. Allow without "+ c "
1	(c)		$(y =) 3x^2 - 5x + 5$	M1	1.1	M1 for attempt integrate $6x - 5$
				A1	1.1	A1 all correct, including $y =$
				[2]		
2			Numerator $\equiv (x+1)(x-2)(2x+3)$	M1	3.1 a	Attempt factorise numerator into 3 linear factors
			Denominator $\equiv (x+1)(x-2)$	M1	1.1	Attempt factorise denominator into 2 linear factors
				M1	1.1	"cancel" two common factors in num & denom
			Ans: $2x + 3$	A1	1.1	Allow no mention of $x \neq -1$ or $x \neq 2$ conditions.
						NB correct answer with no working or partial working: 4 marks
				[4]		SC: Answer $x + \frac{3}{2}$ B3
			Alternative method		1	
			2x + 3	M1		Attempt long division by $x^2 - x - 2$ or by $x + 1$ or by $x - 2$
			$x^2 - x - 2 \overline{2x^3 + x^2 - 7x - 6}$	A1		Obtain "2x" in quotient
			$2x^3 - 2x^2 - 4x$			
			$\frac{3x^2-3x-6}{3x^2-3x-6}$	A1		Obtain "+ 3" in quotient
			$3x^2 - 3x - 6$			
			-2x + 3	A1		Answer $2x + 3$ clear (not just in the division sum)

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(Questi	on	Answer	Mark	AO	Guidance
3	(a)	(i)	$1 + (-2)(-x) + \frac{(-2)(-3)}{2!}(-x)^2 + \frac{(-2)(-3)(-4)}{3!}(-x)^3$	M1	1.1	Correct expressions for at least three terms. May be implied
			$\equiv 1 + 2x + 3x^2 + 4x^3$	A1 [2]	1.1	cao
3	(a)	(ii)	$(n+1) x^n$	B1 [1]	2.2a	Allow $x^n = (n+1) x^n$
3	(b)		$\frac{1}{1-x}$ oe	B1 [1]	1.1	
3	(c)		$2 + 3x + 4x^{2} + 5x^{3} + \dots$ = 1 + x + x^{2} + x^{3} + + 1 + 2x + 3x^{2} + 4x^{3} + \dots	M1	3.1a	
			$= \frac{1}{1-x} + \frac{1}{(1-x)^2} = \frac{(1-x)+1}{(1-x)^2}$	M1	3.1a	Their (b)(i) + $\frac{1}{(1-x)^2}$ and attempt single term
			$=\frac{2-x}{\left(1-x\right)^2}$	A1	1.1	cao Unsupported answer, no marks
			$(r - r)(1 - r)^{-2}$	[3]		
			$(a - x)(1 - x)^{2}$ $a + 2ax + 3ax^{2} + 4ax^{3} + \dots$ $-(x + 2x^{2} + 3x^{3} + 4x^{4} + \dots)$ $a = 2$ $\frac{2-x}{(1-x)^{2}}$	MI M1		
			Justification for all terms up to infinity	A1		
						NB other correct methods exist

Mark Scheme

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(Questio	on	Answer	Mark	AO	Guidance
4			$\frac{\mathbf{DR}}{3\sin^4\phi + \sin^2\phi - 4} = 0$			
			$(3\sin^2\phi + 4)(\sin^2\phi - 1) = 0$	B 1	2.1	Attempt to solve QE in $\sin^2 \phi$ or QE in <i>u</i> with $u = \sin^2 \phi$ soi Must see method
			$\sin^2 \phi = -\frac{4}{3}$ or $\sin^2 \phi = 1$ (or $\sin \phi = 1$)	B1	1.1	May be implied from $x = \sin^2 \phi$ and $x = -\frac{4}{3}$ or 1
			$\sin^2 \phi = -\frac{4}{3}$ is impossible	B 1	2.3	oe, eg sin $\phi \neq \sqrt{-\frac{4}{3}}$ Not with incorrect reason, eg sin ² $\phi = \frac{16}{9} > 1$
			$\phi = \sin^{-1} (\pm 1)$	M1	1.1	solve for ϕ Allow $\phi = \sin^{-1}(1)$, may be implied
			$\phi = \frac{1}{2}\pi, \frac{3}{2}\pi$ No extras within range Allow "correct" extras outside range	A1	2.2a	Both. dep $\sin^2 \phi = -\frac{4}{3}$ and $\sin^2 \phi = 1$ (or $\sin \phi = 1$) seen
				[5]		SC $\phi = \frac{1}{2}\pi$, $\frac{3}{2}\pi$ with no working: B2
5	(a)		$n^2 - 1$ or $n^2 + 1$ is even			B1 for <u>any</u> of these. Numerical examples insufficient
5	(u)		OR n^2 is odd or $n^2 = 2k + 1$ (<i>k</i> integer)			Ignore extra, eg $\frac{n^2+1}{2} > 0 \Rightarrow n^2 > -1$ or $n > \sqrt{-1}$ or $n \neq -1$
			OR $\frac{n^2 - 1}{2} > 0$ or $\frac{n^2 - 1}{2} \ge 1$ or $n^2 \ge 3$	B1	2.4	Allow ≥ 0 for this mark
			Assuming <i>n</i> is a positive integer:			Not assuming <i>n</i> is a positive integer:
			<i>n</i> is odd oe eg $n = 2k + 1$ (<i>k</i> integer)	B1	2.2a	
			$n > 1$ (or $n < -1$) or $ n > 1$ or $n \ge \sqrt{3}$ Not $n \ge 0$	B1	2.2a	$n = \sqrt{\text{odd integers} > 1}$ or $n = \sqrt{3}$, $\sqrt{5}$ etc oe B2 indep
			NOT $n > \pm 1$ but ignore this if followed by			
			correct, eg $ n > 1$			2nd and 3rd B1 marks are independent & can be gained without
				[3]		explanation
=			$2 \cdot (n^2 - 1)^2$		21-	$(n^2+1)^2 (n^2-1)^2$
5	(D)		$n^2 + (\frac{n}{2})^2$	NII	3. 1a	$\left(\frac{n+1}{2}\right)^2 - \left(\frac{n-1}{2}\right)^2$ correct expression
			$= n^2 + \frac{n^4 - 2n^2 + 1}{4} = \frac{n^4 + 2n^2 + 1}{4}$			$= \frac{n^4 + 2n^2 + 1}{4} - \frac{n^4 - 2n^2 + 1}{4} = \frac{4n^2}{4}$
			$=\left(\frac{n^2+1}{2}\right)^2$	A1	1.1	$= n^2$ Correctly obtained
				[2]		

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(Question		Answer	Mark	AO	Guidance		
5	(b)	ctd	$n^{2} + \left(\frac{n^{2} - 1}{2}\right)^{2} = \left(\frac{n^{2} + 1}{2}\right)^{2}$	M1				
			$n^{2} + \frac{n^{4} - 2n^{2} + 1}{4} = \frac{n^{4} + 2n^{2} + 1}{4}$ $4n^{2} + n^{4} - 2n^{2} + 1 = n^{4} + 2n^{2} + 1$	A 1				
6			LHS = $\sqrt{2} (\cos 2\theta \cos 45^\circ - \sin 2\theta \sin 45^\circ)$	M1	3.1 a	correct use of $\cos(A+B)$ formula		
			$\equiv \sqrt{2} \times \frac{1}{\sqrt{2}} (\cos 2\theta - \sin 2\theta) \text{ or } (\cos 2\theta - \sin 2\theta)$	B1	1.1	$\cos 45^\circ$ or $\sin 45^\circ = \frac{1}{\sqrt{2}}$ seen or implied		
			$\equiv \cos^2\theta - 2\sin\theta\cos\theta - \sin^2\theta$	A1	2.2a	correctly obtained – use of double angle formulae clear		
			Alternative method RHS $\equiv \cos 2\theta - \sin 2\theta$	M1				
			$\equiv \sqrt{2}\left(\frac{1}{\sqrt{2}}\cos 2\theta - \frac{1}{\sqrt{2}}\sin 2\theta\right)$			or $R\cos \alpha = 1$, $R\sin \alpha = 1$, $R^2 = 2$, $\tan \alpha = 1$, $\alpha = 45^{\circ}$		
			$\equiv \sqrt{2} \left(\cos 2\theta \cos 45^{\circ} - \sin 2\theta \sin 45^{\circ} \right)$	M1				
			$\equiv \sqrt{2}\cos(2\theta + 45^{\circ})$	A1				
				[3]				
7	all		Allow <i>a</i> and <i>b</i> without "squiggles" beneath					
7	(a)		Length of <i>AB</i> oe	B1	1.2	Magnitude of <i>AB</i> or distance from <i>A</i> to <i>B</i> Allow Magnitude of <i>AB</i> Not magnitude of $ \mathbf{a} - \mathbf{b} $ or magnitude of $\mathbf{a} - \mathbf{b}$ Not distance from <i>a</i> to <i>b</i> Not distance from position vector <i>A</i> to position vector <i>B</i>		
7	(b)		Midpoint of <i>AB</i> oe	B1	1.2	or Halfway between A and B Allow Midpoint of \overline{AB} Must refer to A and B, not a and b Not Midpoint of the vectors		
7	(c)	(i)	$\frac{1}{2}(\mathbf{a} + \mathbf{b})$	R1	2.22	L		
				[1]	2.2a			
7	(c)	(ii)	$\frac{1}{2} \mathbf{a} - \mathbf{b} $ oe	B1 [1]	2.2a			

Question		n	Answer	Mark	AO	Guidance
7	(d)		Centre is (3, 2)	B1	1.1	Allow this mark for (3, 2) or $\begin{pmatrix} 3 \\ 2 \end{pmatrix}$ or $\frac{1}{2} \begin{pmatrix} 6 \\ 4 \end{pmatrix}$ oe seen
			$r^2 = 10$ or $r = \sqrt{10}$ or 3.16 (3 sf)	B 1	1.1	May be implied by answer May be implied by answer. Must imply radius
				M1	1.1	M1 for $(x - a)^2 + (y - b)^2 = r^2$ for any non-zero numerical a, b and r
			$(x-3)^2 + (y-2)^2 = 10$	A1	1.1	A1 for all correct. ISW
				[4]		
8	(a)		<u>Summary scheme</u> Attempt separate variables using $(100 - P)$ Correct integral, but allowing	M1	3.1 a	
			100 - P or $(P - 100)$ or $(100 - P)$	A1	1.1	Allow without $+ c$
			Attempt $t = 0$, $P = 2000$ to find c or A or $e^{\pm c}$	M1	3.4	dep M1
			$c = -\ln 1900$ or $A = 1900$ or $e^{\pm c} = 1900$ OR Allow $c = \ln 1000$ or $\ln(-1000)$			
			OR Allow $c = 111900$ or $-11(-1900)$			
			or A or $e^{\pm c} = -1900$ or $-\frac{1}{1900}$	A1	3.4	dep M1M1
			Attempt make P the subject	M1	3.4	dep M1M1A1
			Correct use of mod & change to $P - 100$	M1	2.1	
			$P = 1900e^{-t} + 100$	A1	1.1	dep M1A1M1A1M1M1 ie dep all correct working seen
			Examples of correct methods			
			$\frac{\mathrm{d}P}{100-P} = \mathrm{d}t$	M1		
			$-\ln 100 - P = t + c$ or $ 100 - P = Ae^{-t}$	A1		
			Substitute $t = 0, P = 2000$	M1		
			$\Rightarrow c = -\ln 1900$ or $A = 1900$	A1		
			$\ln \frac{ 100-P }{1900} = -t \qquad \text{or } 100-P = 1900e^{-t}$			
			$\frac{P-100}{1900} = e^{-t}$			
			D 1000 -t 100	M1		
			$P = 1900e^{-i} + 100$	Al		
				AI		

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	Questic	n	Answer	Mark AO		Guidance		
8	(a)	ctd	$\frac{dP}{P-100} = -dt$ $\ln(P-100) = -t + c \text{or } P - 100 = Ae^{-t}$ Substitute $t = 0, P = 2000$ $\Rightarrow c = \ln 1900 \text{ correct} \text{or } A = 1900$ $\ln(P-100) = -t + \ln 1900 \text{ or } P - 100 = 1900e^{-t}$ $\frac{P-100}{1000} = e^{-t}$	M1 M1 A1 M1 A1				
			$P = 1900e^{-t} + 100$	M1 A1				
			Example of incorrect methods			(
			$\frac{dP}{100-P} = dt$ -ln(100 - P) = t + c or 100 - P = Ae ^{-t} 100 - P = e ^{-t-c} Substitute t = 0, P = 2000 $\Rightarrow e^{-c} = -1900$ or A = -1900 100 - P = -1900e ^{-t} oe No change to P - 100 P = 1900e ^{-t} + 100	M1 A1 M1 A1 M0 M1 A0		Correct answer but incorrectly obtained, not using modulus		
			$\frac{dP}{100-P} = dt$ $\ln(100 - P) = t + c$ Substitute $t = 0, P = 2000$ $\ln(-1900) = c$ $\ln(100-P) = t + \ln(-1900)$ $100 - P = -1900e^{t}$ No change to $P - 100$ $P = 100 + 1900e^{t}$	M1 A0 M1 A1 M0 M1 A0				

(Question			Answer	Mark	AO	Guidance
8	(b)		(Starts at 2000)	Decreases Approaches 100	B1f B1f [2]	3.4 3.4	B1 for correct process or ft (a) dep (a) includes exponential B1 for correct limit or ft (a) dep (a) includes exponential
9	(a)		(40000 × 0.002 =)	80	B1 [1]	1.1	
9	(b)		Frequency per £	or No. of cars per £	B1	1.1	Allow cars / £Allow as fractionNOT cars / priceNOT cars / money
9	(c)		Show fds for four £50000 - £90000	separate classes within	B1	2.3	Make price intervals smaller Show the median (or similar) Include more bars Give a title Explain y-axis better or give units of f.d. Give the frequencies
9	(d)		20		B1f [1]	1.1	or (a) ÷ 4

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Questio	n Answer	Mark	AO	Guidance
10	H ₀ : $p = 0.9$, where $p = P(a \text{ random customer is satisfied})$ H ₁ : $p < 0.9$	B1 B1	1.1 2.5	Allow rounded or truncated to 2 sf throughout or p is proportion satisfiedAllow other lettersOR $p = 90\%$, where p is % of customers satisfiedSubtract B1 for each error eg: 2-tail2-tailB1B0Use of \leq with definitionB1B0Not include value 0.9B0B0not in terms of parameterB1B0Ho = 0.9 etc:
	$X \sim Bin(15, 0.9) \text{ and } X \le 10 \text{ or } 11 \text{ or } 12$ (condone < or = or > or ≥)	M1	3.3	Stated or implied eg by 0.0556 or 0.184 or 0.0127 or 0.944 or 0.816 or 0.987 or 0.0428 or 0.129
	$P(X \le 11)$ oe $P(X > 11)$ oe $= 0.944$	A1	3.4	BC cao
	Comp 0.05 Comp 0.95	A1	1.1	Dep 0.0556 or 0.184 or 0.0127 or 0.944 or 0.816 or 0.987 Must be correct comparison, eg not 0.944 comp with 0.05
	Alternative method for middle two A-marks $P(X \le 10) = 0.0127$ $P(X \le 11) = 0.0556$ Hence rejection region is $X \le 10$ (or $X < 11$) or critical value is $X = 10$	A1 A1		Both needed Dep on M1
	Do not reject H ₀ Condone Accept H ₀ There is insufficient evidence that Pierre is overconfident (or that < 90% are satisfied) oe, eg There is insufficient evidence that Yvette's suspicion is correct	M1 A1f [7]	1.1 2.2b	 Dep 0.0556 or 0.184 or 0.0127 (2 sf) or P(X ≤ 10 or 11 or 12)seen or 0.944 or 0.816 or 0.987 P(X > 10 or 11 or 12) seen And dep correct comparison, eg, not 0.944 comp with 0.05 In context. Not definite. Full statement Not: There is evidence that Pierre is not overconfident oe
	N~Bin: $\mu = 13.5, \mu < 13.5$ B1B0N(13.5, 1.35) & X = 11.5 or 11M1 $p = 0.0426$ A1compare 0.05A1ConclusionM0A0) 1 1)		dep defined μ. If undefined: B0B0 soi dep 0.0426 or 0.0157

Question		on	Answer	Mark	AO	Guidance
10	ctd		2-tail: $H_0: p = 0.9$ defined p $H_1: p \neq 0.9$ X~Bin(15, 0.9) and X \leq 11 or 12 (condone < or = or > or \geq) P(X \leq 11) oe = 0.0556 Comp 0.025 Conclusion			Stated or implied eg by 0.0556 or 0.184 or 0.944 or 0.816 or 0.0428 or 0.129 Dep 0.0556 or 0.184
11	(a)		(mean =) 201 (3 sf) (sd =) 60.7 (3 sf)	B1 B1 [2]	1.1 1.1	Allow 60.8
11	(b)		0.364 (3 sf)	B1 [1]	3.4	
11	(c)		P(X < 160) = 0.252(49) $x_1 = \Phi^{-1}(0.6 + 0.25249')$ = 262.83 (5 sf) ISW	B1 M1 A1 [3]	3.4 1.1 1.1	soi, eg by $P(X > 160) = 0.748$ or 0.747 or by 0.147 or 0.148 T&I: correct answer scores B1M1A1, otherwise max B1 SC Answer 263 with correct working: B1M1A0 SC Answer 263 with inadequate working: B1 only
11	(d)		112 and 288 are within 2 sd from mean (no working needed) P(X < 112) = 0.0708, which is > 0.025 or > 0.0013 or > 0	B1	3.5a	or $\mu + 2\sigma = 320$ ($\mu + 3\sigma = 380$) which is > than 288 or P(112< $M < 288$) = 0.858 which is < than 0.95 (or 0.99) or $p = 0.858$, but model suggests $p = 1$ NOT 0.858 alone B0
11	(e)		Reduce σ $288 - 200 = 2\sigma$ or $288 - 200 = 3\sigma$ or $288 - 112 = 4\sigma$ or $288 - 112 = 6\sigma$ $\sigma = 44$ $\sigma = 29.3$ or about 30	B1 B1 [2]	3.5c 3.3	May be implied by value of σ Allow more precise correct methods Allow σ between 25 and 50. No working needed B1B1 or σ^2 between 625 and 2500

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	Questic	on	Answer	Mark	AO	Guidance		
12	(a)		H ₀ : $\mu = 45.7$, where $\mu =$ mean of all new journey times H ₁ : $\mu < 45.7$	B1 B1	1.1 2.5	Allow "where μ = mean journey time" Allow different letters Subtract B1 for each error eg: use of "p" unless defined B0B0 2-tail B1B0 μ = sample mean implied B1B0 undefined μ B1B0 Not include value 45.7 B0B0 not in terms of parameter B1B0 H ₀ = 45.7 etc: B0B0		
12	(b)		N(45.7, $\frac{5.6^2}{30}$) and probability = 0.025 soi P($\overline{X} < a$) = 0.025 or $a = \Phi^{-1}(0.025)$ a = 43.7 (3 sf) (43.696) Rejection region is (\overline{X}) < 43.7 (3 sf) or (\overline{X}) < 43.6 with explanation	[2] M1* M1 A1f A1 [4]	3.3 1.1 1.1 1.1	or N(45.7, $\frac{392}{375}$) or N(45.7, 1.045) and probability = 0.025 soi soi Dep M1 Allow \leq . Answer (\overline{X}) < 34.7 SC B1 (from not \div by $\sqrt{30}$) Correct answer with inadequate or no working: SC B2 If (a) μ > 45.7, allow (\overline{X}) > 47.7, M1M1A1A0		
13	(a)	(i)	P(AA or BAA) = $0.4^2 + 0.6 \times 0.4^2$ oe = 0.256 or $\frac{32}{125}$	M1 A1 [2]	3.1b 1.1	allow M1 for either 0.4^2 (×) or 0.6×0.4^2 (×)		
13	(a)	(ii)	ABA or BAB P(ABA or BAB) = $0.4^2 \times 0.6 + 0.6^2 \times 0.4$ 0.24 Alternative method $1 - ("0.256" + 0.6^2 + 0.4 \times 0.6^2)$ = 0.24	M1 M1 A1 M1 A1 [3]	3.1b 1.1 1.1	both seen or implied M1 for either $0.4^2 \times 0.6$ or $0.6^2 \times 0.4$ M1 for $1 - P(A \text{ wins or B wins})$ attempted M1 for $1 - ("0.256" (+))$ or $1 - (() + 0.6^2 + 0.4 \times 0.6^2)$ NB $0.4 \times 0.6 = 0.24$: M0M0A0		
13	(b)			M1 M1 A1 [3]	3.1b 2.1 1.1	ft (a)(i)&(ii) ft (a)(i)&(ii) ie $\frac{(a)(i)}{1-(a)(ii)}$ cao S ₅ = 0.337 SC B1, but with added comment M1M1A1		

Question			Answer	Mark	AO	Guidance
14	(a)	(i)	The actual number of extra pupils determines the number of places needed Shows how many new students there will be Shows trend so LA can provide accordingly Need to know expected number of pupils	B1 [1]	2.2b	The existing numbers are already catered for Increase in provision Not Need to know increase in proportion of pupils
14	(a)	(ii)	Wigan Increase in number is greatest there	B1 B1 [2]	2.2b 2.2b	Allow "Wigan and Bolton" Ignore mention of % increase. Ignore extras.
14	(a)	(iii)	 E.g. all those in this category stay in the LA Populations continue growing at same rate Populations all growing at same rate The population increases consistently NOT Increase has been steady All LAs have the same teacher/pupil ratio All LAs have same need for teachers in 2011 	B1 [1]	2.2b	No decrease in population Children born in that LA will go to school in that LA Assume no great influx or outflow of children after 2011. The LAs are not currently understaffed Ignore extra eg "between 2001 & 2011"
14	(b)		Manchester and SalfordB1Highest % or absolute increaseB1depManchester and LiverpoolB1The two highest in 2011B1depSC Manchester (alone), Highest % or absolute increase:B1B0	B1 B1 [2]	2.2b 2.4	Wigan and BoltonB1Highest numbers in 2011 except Manchester and Liverpool, which are very largeB1depSalford and TraffordB1They have the largest absolute (or %) increase, but are small (or not huge like Manchester)B1dep
15	(a)		DR $\frac{15}{64} \times \frac{2^2}{2!}$ oe eg $\frac{15}{64} \times \frac{4}{2}$ (= $\frac{15}{32}$ AG)	B1	1.1	Must see this expression and result
				[[1]		

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Questio	n Answer	Mark	AO	Guidance
15 (b)	DR 2, 2, 5 2, 3, 4 3, 3, 3	M1	3.1a	Any two seen, with no more than 2 extra different combinations. eg 0, 4, 5 and 0, 5, 4 count as <u>one</u> extra
	$P(X_{1} + X_{2} + X_{3} = 9) =$ $3 \times (\frac{15}{32})^{2} \times \frac{5}{80} + 6 \times \frac{15}{32} \times \frac{5}{16} \times \frac{5}{32} + (\frac{5}{16})^{3}$ $0.0412 + 0.1373 + 0.0305$ $3 \times \frac{225}{16384} + 6 \times \frac{375}{16384} + \frac{125}{4096}$ $\frac{675}{16384} + \frac{1125}{8192} + \frac{125}{4096} \qquad (= 0.209045)$ $P(X_{1} + X_{2} + X_{3} = 9 \text{ and at least } 1 X \text{ value } = 2)$ $= 3 \times (\frac{15}{32})^{2} \times \frac{5}{80} + 6 \times \frac{15}{32} \times \frac{5}{16} \times \frac{5}{32} \qquad (= 0.178528)$ $\frac{'0.178528'}{'0.209045'}$ $= 0.854 (3 \text{ sf}) \text{ or } \frac{117}{137}$	M1 M1 M1 M1 A1	2.1 2.1 1.1 2.1 2.2a	 M2: ≥ 1 correct product actually seen & all three products correct M1: 1 correct product seen or all correct except omission of, or incorrect, multiple(s) or all three results or total correct, but without working Allow M1 for 1 correct product or omit, or incorrect, multiple(s) or ft their probabilities from their previous calculation ÷ their attempted probs of correct events
	$P(X_1 + X_2 + X_3 = 9 \text{ and no } X \text{ value} = 2)$ = $(\frac{5}{16})^3$ (= 0.030518 or $\frac{125}{4096}$) 1 - $\frac{0.030518}{0.209045}$ = 0.854 (3 sf) or $\frac{117}{137}$	M1 M1 A1 [6]		ft their P(3, 3, 3) \div their attempted probabilities of correct events & subtract from 1 NB 1 – $(\frac{5}{16})^3$ alone scores M1

Mark Scheme

Question		on	Answer	Mark	AO	Guidance
15	(c)		P(two 2's in nine vales of X) or 0.094466 or ${}^{9}C_{2} \times (1 - \frac{15}{32})^{7} \times (\frac{15}{32})^{2}$	M1	3. 1a	soi eg by ⁹ C ₂ seen
			P(two 2's in nine vales of X) × P(X = 2) or 0.094466 × $\frac{15}{32}$ or ${}^{9}C_{2}$ × $(1 - \frac{15}{32})^{7}$ × $(\frac{15}{32})^{3}$	M1	2.1	soi NB $\left(\frac{17}{32}\right)^7 \times \left(\frac{15}{32}\right)^3$ scores 0, unless multiplied by 9C_2
			0.0443 (3 sf)	A1	1.1	
				[3]		

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